(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID: 1250 Roll No.

### B. Tech.

# (SEM. III) ODD SEMESTER THEORY EXAMINATION 2013-14 SIGNALS AND SYSTEMS

Total Marks: 100

Note: -Answer all the questions.

#### SECTION-A

1. Attempt all parts:

Time: 3 Hours

 $(10 \times 2 = 20)$ 

(a) Determine the fundamental period of the signal:

$$x(t) = 3 \sin(7t + 2) - 4 \cos(4t + 1)$$
.

(b) Consider a discrete-time system with input x [n] and outputy [n]:

$$y[n] = x[n+2] - x[n-2].$$

Is this system Linear?

- (c) Determine the Z-Transform of  $x [n] = a^{-1}u [-n]$ .
- (d) Find Laplace Transform of  $x(t) = \sum_{k=0}^{\infty} \delta(t-kT)$
- (e) Prove the time scaling property of Fourier transform.

(f) For the following frequency response of a causal and stable LTI System:

$$H(jw) = \frac{1-jw}{1+jw}.$$

Show that |H(jw)| = A, and determine the value of A.

- (g) Consider a LTI System with step response  $y(t) = e^{-t} u(t)$ . Determine the output of this system to the input x(t) = u(t-1) - u(t-3).
- (h) Find the Fourier transform of the Signal:  $X(t) = e^{\alpha t} u(-t), a > 0.$
- (i)  $X(s) = \frac{s^2 + 5s + 7}{s^2 + 3s + 2}$ , Determine the value of  $x(\infty)$ .
- (j) Sketch the given signal:

$$x(t) = r(t) u(3-t)$$
.

## SECTION-B

Attempt any three parts:

 $(3 \times 10 = 30)$ 

(a) (i) Determine the impulse response of the Discrete Time System:

$$y(n) - 3y(n-1) + 2y(n-2) = x(n) + 3x(n-1) + 2x(n-2).$$

(ii) Let x(t) = u(t-3) - u(t-5) and  $h(t) = \overline{e}^{3t} u(t)$ . Compute y(t) = x(t) \* h(t).

- (b) (i) Define Ideal frequency Selective filter. Explain time domain properties of ideal frequency selective filter.
  - (ii) State and prove Sampling theorem and discuss the effect of under sampling.
- (c) (i) Find the Inverse Laplace Transform of:

$$X(s) = \frac{2}{(s+4)(s-1)}$$
 If the region of convergence is:

- (a) -4 < Re(s) < 1
- (b) Re(s) > 1
- (c) Re(s) < -4.
- (ii) Sketch and determine the convolution of the following signals:

$$x(t) = \pi \left(\frac{t-1}{3}\right)$$
;  $h(t) = u(t-5)$ .

- (d) (i) Find the Unilateral Z-Transform of:  $x[n] = [a^n Sin w_o n] u[n].$ 
  - (ii) If  $x(z) = \frac{2z}{3z^2 4z + 1}$ , find x(n);  $n \ge 0$ . Given that ROC of x(z) is |z| > 1.
- (e) Realize  $H(s) = \frac{s(s+2)}{(s+1)(s+3)(s+4)}$ , by canonic direct form II.

## SECTION-C

Note: - Attempt all questions in this Section.

3. Attempt any one part:

 $(5 \times 10 = 50)$ 

(a) Impulse-Train sampling of x[n] is used to obtain:

$$g[n] = \sum_{k=-\infty}^{\infty} x[n] \ \delta[n-KN].$$

If  $x(e^{jw}) = 0$  for  $\frac{3\pi}{7} \le |w| \le \pi$ , determine the largest value

for the sampling interval N which ensures that no aliasing takes place while sampling x [n].

(b) Determine whether or not each of the following continuoustime signals are periodic. If the signal is periodic, determine its fundamental period:

(i) 
$$x(t) = 3 \cos(4t + \pi/3)$$

(ii) 
$$x(t) = e^{j(\pi t - 1)}$$

(iii) 
$$x(t) = [\cos(2t - \pi/3)]^2$$

(iv) 
$$x(t) = \cos^2 \frac{\pi}{8}t$$

(v) 
$$x(t) = \sum_{n=-\infty}^{\infty} e^{-(2t-n)} u(2t-n)$$
.

- 4. Attempt any one part:
  - (a) Find the Z-Transform x(z) and sketch the pole-zero plot with the ROC of following sequence:

$$x[n] = \left(\frac{1}{3}\right)^n u[n] + \left(\frac{1}{2}\right)^n u[-n-1].$$

- (b) Using the power series expansion technique, find the inverse Z-Transform of the following x (z):
  - (i) Using Long Division Method:

$$X(z) = \frac{z^2 + 2z}{z^3 - 3z^2 + 4z + 1} |ROC|z| > 1$$

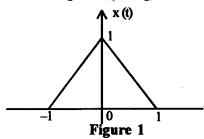
- (ii)  $X(z) = \log_{a} (1 + az^{-1}) ROC |z| > a$ .
- 5. Attempt any one part:
  - (a) Consider a continuous-time LTI System described by:

$$\frac{\mathrm{d}y(t)}{\mathrm{d}t} + 2y(t) = x(t)$$

Using the Fourier transform, find the output y (t) of the following input signal:

 $x(t) = e^{-t} u(t)$  and determine the frequency response H ( $e^{jw}$ ) of the system.

(b) Consider the signal x(t) in figure 1.



- (i) Find the Fourier transform x (jw) of x (t).
- (ii) Sketch the signal:

$$y(t) = x(t) * \sum_{k=-\infty}^{\infty} \delta(t-4k).$$

- Attempt any one part:
  - (a) Consider two Right-Sided Signals x(t) and y(t) related through the differential equations:

$$\frac{dx(t)}{dt} = -2y(t) + \delta(t) \text{ and } \frac{dy(t)}{dt} = 2x(t).$$

Determine y(s) and x(s) alongwith their regions of Convergence.

(b) The input x [n] and output y [n] of a causal LTI system are related through the block diagram representation shown in figure 2:

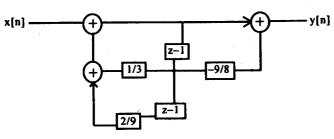


Figure 2

- Write a difference equation relating y [n] and x [n].
- Explain the Stability Analysis of the given system as shown in figure 2.
- Attempt any two parts:
  - (a) Let x (t) be a signal with Nyquist rate w<sub>o</sub>. Determine the Nyquist rate for the following signals:

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(i) 
$$x(t) + x(t-1)$$

(ii) 
$$x^2$$
 (1).

(b) Suppose that  $x(t) = e^{-(t-2)} u(t-2)$  and h(t) is shown in figure 3:

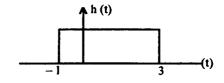


Figure 3

Verify the convolution property for this pair.

Obtain the Fourier series for the wave form shown in figure 4:

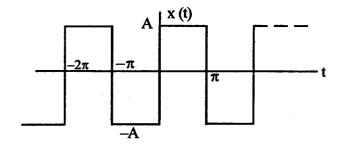


Figure 4

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